

Cambridge Assessment International Education

Cambridge International Advanced Subsidiary and Advanced Level

MATHEMATICS

Paper 2

MARK SCHEME

Maximum Mark: 50

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the October/November 2019 series for most Cambridge IGCSE™, Cambridge International A and AS Level components and some Cambridge O Level components.



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Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always whole marks (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- · marks are awarded when candidates clearly demonstrate what they know and can do
- · marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

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Cambridge International AS/A Level – Mark Scheme

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Mark Scheme Notes

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

- Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- **B** Mark for a correct result or statement independent of method marks.
- DM or DB When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly, when there are several B marks allocated. The notation DM or DB is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
 - FT Implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only.

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Abbreviations

AEF/OE	Any Equivalent Form (of answer is equally acceptable) / Or Equivalent
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
CAO	Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)
CWO	Correct Working Only
ISW	Ignore Subsequent Working
SOI	Seen Or Implied
SC	Special Case (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)
WWW	Without Wrong Working
AWRT	Answer Which Rounds To

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Question	Answer	Marks	Guidance
1	Divide at least as far as the x term in the quotient	M1	Allow use of $(x^2 + 2)(x^2 + ax + b) + cx + d$
	Obtain at least $x^2 - 3x$	A1	
	Obtain $x^2 - 3x + 3$ and remainder 5	A1	
		3	

Question	Answer	Marks	Guidance
2(i)	State or imply non-modular equation $(4x + 5)^2 = (x - 7)^2$ or pair of different linear equations	B1	
	Attempt solution of 3-term quadratic equation or pair of linear equations	M1	
	Obtain $\frac{2}{5}$ and -4	A1	SC For $x = -4$ only, from correct work, allow B1
		3	
2(ii)	Apply logarithms and use power law for $2^y = k$ where $k > 0$ from (i)	M1	
	Obtain –1.32 only	A1	AWRT
		2	

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Question	Answer	Marks	Guidance	
3	ln y = ln k + a ln x	B1	SOI	
	Equate gradient of line to a	M1		
	Obtain $a = -1.39$	A1	OE	
	Substitute appropriate values into a correct equation to find $\ln k$	M1		
	Obtain $\ln k = 4.266$ and $k = 71.2$	A1	SC1 for gradient = -1.39 and no other relevant working	
	Alternative method for question 3			
	ln y = ln k + a ln x	B1	SOI	
	$3.96 = \ln k + 0.22a$	M1	For one correct equation	
	$2.43 = \ln k + 1.32a$	M1	For a second correct equation and attempt to solve to find one unknown	
	Obtain $a = -1.39$	A1	OE	
	Obtain $\ln k = 4.266$ and $k = 71.2$	A1	SC1 for gradient = -1.39 and no other relevant working	
	Alternative method for question 3			
	$e^{3.96} = k \times 0.22^a$ and $e^{2.43} = k \times 1.32^a$	B1		
	Apply a correct method to obtain a	M1		
	Obtain $a = -1.39$	A1	OE	
	Substitute appropriate values into a correct equation to find k	M1		
	Obtain $k = 71.2$	A1	AWRT	
		5		

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	October/November 2019
Guidance	,
attempt at x_3	
to exactly 4 sf	
st x_5	

Question	Answer	Marks	Guidance
4(i)	Use iteration correctly at least once	M1	Must see correct attempt at x_3
	Obtain final answer 1.359	A1	
	Show sufficient iterations to 6 sf to justify answer or show sign change in interval [1.3585, 1.3595]	A1	Answer required to exactly 4 sf Must see to at least x_5
		3	
4(ii)	Form correct equation in x (or α)	B1	$x = \frac{x}{\ln 2x} \text{ OE}$
	Obtain ½e	B1	
		2	

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Question	Answer	Marks	Guidance
5	Differentiate using the product rule	*M1	Must have u and v correct in a correct formula with $\frac{du}{dx} = 2$ and $\frac{dv}{dx} = me^{-\frac{1}{2}x}$
	Obtain correct $2e^{-\frac{1}{2}x} - \frac{1}{2}e^{-\frac{1}{2}x}(2x+5)$	A1	OE
	Equate first derivative to zero and solve for x	DM1	Solution must come from linear terms
	Obtain $x = -\frac{1}{2}$ only	A1	
	Obtain $4e^{\frac{1}{4}}$ or exact equivalent only	A1	
		5	

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Question	Answer	Marks	Guidance
6(a)	Obtain $\frac{3}{2} \ln x$ or $\frac{3}{2} \ln(2x)$ or $\frac{3}{2} \ln(kx)$	B1	
	Use subtraction law of logarithms correctly, showing sufficient detail	M1	$\ln 216 - \ln 8 = \ln \left(\frac{216}{8}\right)$
	Use power law of logarithms correctly	M1	$n\ln\left(kx\right) = \ln\left(kx\right)^n$
	Confirm ln 27 with sufficient working and no incorrect working	A1	AG
		4	
6(b)	Use appropriate identity to express integrand in form $k_1 + k_2 \cos 3x$	*M1	$k_1 \neq 0$. Allow $2 \times \frac{3}{2}x$ for $3x$
	Obtain correct $2-2\cos 3x$	A1	
	Integrate to obtain form $k_3x + k_4 \sin 3x$	DM1	
	Obtain correct $2x - \frac{2}{3}\sin 3x$	A1	
	Use limits to obtain $\frac{1}{3}\pi - \frac{2}{3}$ or exact equivalent	A1	
		5	

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Question	Answer	Marks	Guidance
7(i)	Obtain $\frac{dx}{d\theta} = 6\cos 2\theta$	B1	
	Obtain $\frac{dy}{d\theta} = 4\sec^2 2\theta$	B1	
	Divide $\frac{dy}{d\theta}$ by $\frac{dx}{d\theta}$ with θ equated to $\frac{1}{6}\pi$	M1	
	Obtain $\frac{16}{3}$ or exact equivalent	A1	Allow FT on A1 if $\frac{dx}{d\theta} = 3\cos 2\theta$ and $\frac{dy}{d\theta} = 2\sec^2 2\theta$
		4	
7(ii)	Equate expression for $\frac{dy}{dx}$ to 2 with only one trigonometry ratio used	*M1	Either $\cos 2\theta$ or $\sec 2\theta$
	Obtain $\cos^3 2\theta = \frac{1}{3}$ or $\sec^3 = 3$	A1	
	Attempt correct steps to find a value of θ from $\cos^3 2\theta = m$, $0 < m < 1$	DM1	
	Obtain $\theta = 0.402$ and no others within the range	A1	AWRT SC: Allow FT if $\frac{dx}{d\theta} = 3\cos 2\theta$ and $\frac{dy}{d\theta} = 2\sec^2 2\theta$
		4	

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Question	Answer	Marks	Guidance
8(i)	State $R = 1.3$ or $\frac{10}{3}$	B1	Not $\sqrt{1.69}$
	Use appropriate trigonometry to find α	M1	AWRT ±1.18 rads, AWRT ±0.391 rads, AWRT ±67.4°, AWRT ±22.6°
	Obtain 67.38 with no errors seen	A1	AWRT
		3	
8(ii)	Carry out correct method to find one value of θ between 0 and 360	M1	
	Obtain 240.6 (or 344.6)	A1	
	Carry out correct method to find second value of θ between 0 and 360	M1	Must be using either degrees throughout or radians throughout for M marks
	Obtain 344.6 (or 240.6)	A1	
		4	
8(iii)	Recognise expression as $[3-2R\cos(\theta+\alpha)]^2$	M1	
	Obtain $[3-2\times(-1.3)]^2$ and hence 31.36 or 31.4	A1	
	Obtain $[3-2 \times 1.3]^2$ and hence 0.16	A1	
		3	

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